

## Numerical Algorithms

Winter semester 2013/2014 Prof. Dr. Carsten Burstedde Philipp Morgenstern



## **Exercise Sheet 9.**

Due date: Tuesday, 21 January.

Exercise 12. Show that the sufficient decrease conditions,

$$\|f(x + \Delta x)\| \le \|f(x) + c_1(D_x f) \Delta x\|, \qquad (2.2.28)$$

$$g(x + \Delta x) \le g(x) + c_1(D_x g) \Delta x, \qquad (2.2.30)$$

with  $0 < c_1 \ll 1$ ,  $f = D_x g$ , are affine invariant.

(5 points)

**Exercise 13.** For  $u : \Omega \to \mathbb{R}$ ,  $g : \mathbb{R} \to \mathbb{R}$  continuously differentiable, derive formally that for the composition  $g \circ u$  we have

$$D_u g = g' \circ u \in \mathbb{R}.$$

(5 points)